

1st August 2023

Mrs L Howie
Widgeham Barn
Poplar Farm
Laxfield Road
Fressingfield
EYE
IP21 5PY

Our Ref: BS/11352
Your Ref: N/A

Dear Mrs Howie,

**Re: Structural Appraisal Report, Proposed Conversion of Existing Workshop,
Widgeham Barn, Poplar Farm, Fressingfield.**

As requested, we visited the above property on the 20th of July 2023. The purpose of the visit was to undertake a visual inspection of the structure to the existing workshop to enable an assessment to be made regarding its suitability for the proposed conversion to an annex/holiday let. Following our visit, we report as follows:

Scope and limitations

Our inspection and the contents of this report are confined to the existing workshop as indicated on the plan below.



We have not inspected those parts of the structure that were inaccessible, covered or unexposed and as such we are unable to confirm these areas are free from defect. We have not inspected the foundations, which as such are beyond the scope of this report.

The discussions and recommendations contained within this report are based upon the proposals as indicated on Hollins Architects drawing 23 64 – 02, dated May 2023.

Observations and comments

The existing single storey workshop is principally of timber frame construction and measures approximately 9m in length, 5.5m in width. External walls support a mono-pitch roof supporting clay pantiles. The height to eaves of the south elevation is approximately 3.0m. The height to eaves of the north elevation is approximately 4.5m.

External walls comprise 50mm wide, 150mm deep timber studs at 600mm centres, supported on a 0.75m high, 228mm wide brickwork plinth, rendered internally. Above the plinth wall, externally the timber frame is clad in black weatherboard. Locally to the west elevation there is no overlap to the cladding, and at this location ply sheathing is evident beneath. External ply sheathing is also evident to the north elevation where locally there is no internal finish. More generally the external walls are clad internally with OSB, with the exception of the west elevation.

No significant deflection or racking was evident to the timber frame external walls. Also, no significant cracking or lateral movement was evident to the plinth brickwork.

The existing roof comprises 50mm wide, 225mm deep timber rafters, supporting clay pantiles. Throughout the workshop the underside of the rafters has been sheathed in OSB or Plywood. Nail spacings indicate the rafters to be at 450mm centres,

No significant deflection or sagging is evident to the existing roof.

The internal wall comprises 100mm thick blockwork, with a single 615mm long, 110mm wide pier at approximately mid-length of the wall. No significant cracking is evident to the internal wall.

Discussions and recommendations

From the limits of our visual inspection the existing workshop appears to be in good condition, without significant cracking to masonry walls, and without significant movement or deflection to the external timber frame and roof.

We have also completed structural calculations considering the existing timber studs forming the external walls, and the timber rafters forming the roof. These calculations also indicate these members to be adequate (see attached).

We would comment that it is likely the existing internal masonry wall does not have a foundation, and as such independent would be required to the proposed mezzanine, as opposed to the beam bearing onto the internal wall as currently indicated on the architectural drawings. This should include supporting posts and new concrete pad foundations. We would comment also that whilst there is no evidence of significant movement or cracking within the existing internal masonry wall, the wall would benefit from buttressing to reduce its slenderness. This could be provided by the new partitions abutting the wall, or the adjacent post supporting the mezzanine.

We would also comment that at present there is no clear connection between the top of the west wall and the roof structure. Whilst there is no evidence of movement between the roof and wall, we would consider it prudent to provide timber noggins between the end rafter and the studwork forming the west wall, and to extend the ply sheathing to the underside of the timber rafters as this currently stops short of the wall.

To the sides of the existing double doors the timber studs are discontinuous. We would recommend that a full height stud is provided to the ends of the existing timber lintel, replacing the short length of stud, with a further two studs beneath the bearing of the timber lintel. These multi-studs are to be bolted together at 500mm centres using M10 diameter grade 4.6 bolts.

Conclusion

In our considered opinion the existing workshop would be suitable for conversion to an annex/holiday let.

As part of a conversion, we would recommend the following:

- Provide independent support to the proposed mezzanine floor.
- Provide buttressing to the existing internal wall, utilising either the new partitions or the new post supporting the mezzanine floor.
- Provide additional connection between the top of the west wall and the roof.
- Provide multi-studs each side of the existing double doors.

All works should be designed and detailed by a Structural Engineer.

We trust that the above report meets with your current requirements, however, should you have any queries, or require any further assistance, please do not hesitate to contact us.

Yours sincerely,

A large black rectangular redaction box covers the signature area, obscuring the name and any handwritten notes or dates.

Barney Simmons
On behalf of Brett Design Partnership Limited

Enc.

DESIGN CALCULATIONS

JOB TITLE: WICKHAM BARN.

JOB REF: 11552

DATE: JULY 23.

ENGINEER: B.S.

PAGE NO. 1, REV:

BRETT DESIGN

Consulting Engineers

4 Maiden Way, Hadleigh, Suffolk IP7 5EH

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PARTNERSHIP

REMARKS

CONSIDER EXISTING TIMBER FRAME TO WORKSHOP.

DESIGN LOADING DATA

KN/m²

Roof - 20° PITCH.

S - ALLOWING GALE PANTHERS -

0.89.

U - SNOW LOADING -

0.75.

EXTERNAL WALL

S - ALL / STRA / PLM / LOADING -

0.5.

ALLOW 1.0 KN/m² WIND LOAD.

LOADING TO WALL SUPPORTING ROOF

KN/m - 1.0 KN/m

$$\text{ROOF - S} = 0.89 \text{ KN/m}^2 \times \frac{6.0 \text{ m}}{2} =$$

2.67

$$\text{U} = 0.75 \text{ KN/m}^2 \times \frac{6.0 \text{ m}}{2} =$$

2.25

$$\text{WALL - S} = 0.5 \text{ KN/m}^2 \times 3.8 \text{ m} =$$

1.9.

4.57. 2.25

AREA REF: TM211765

REVISION DETAILS:

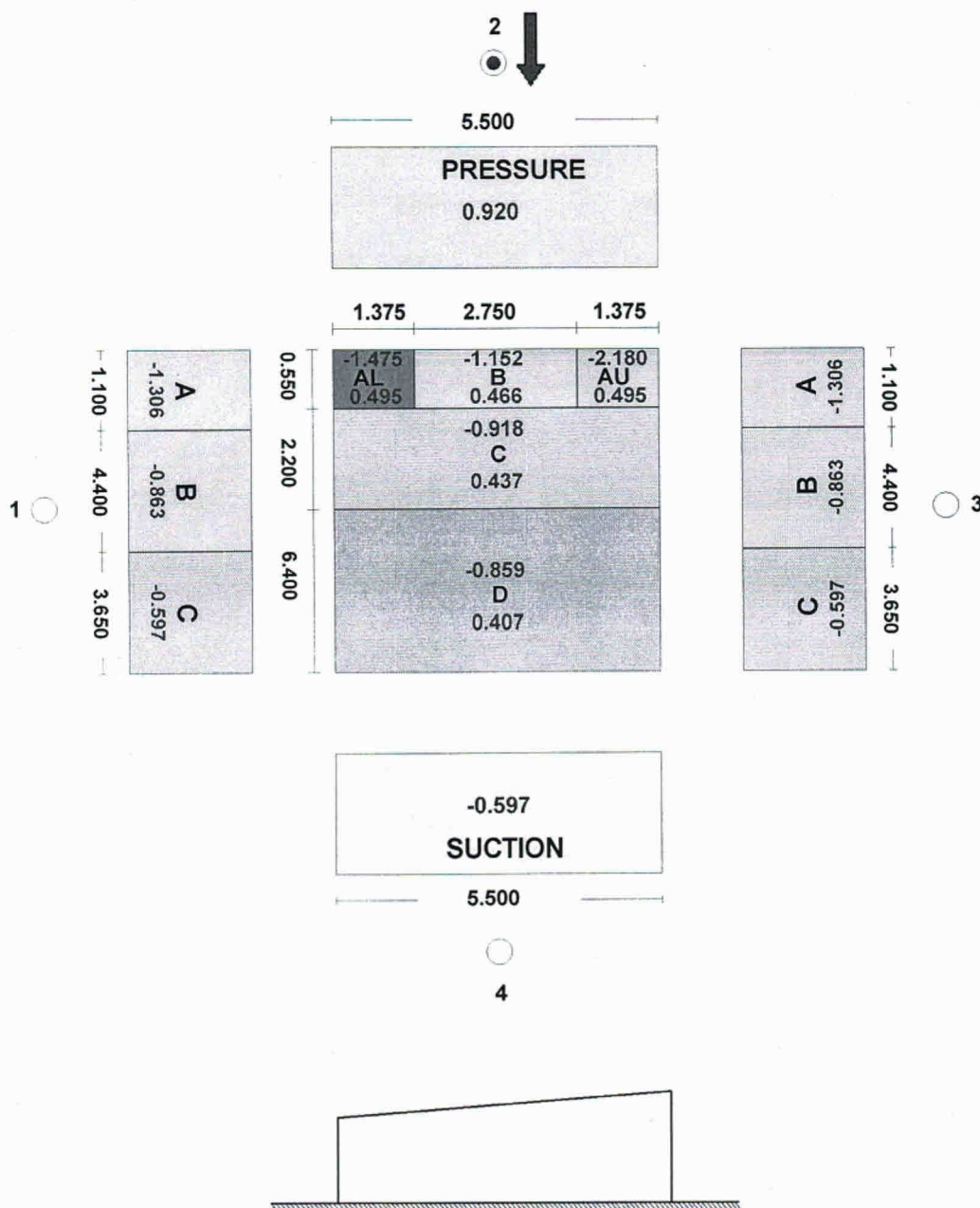


Wind Code Suite

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Job No.
Customer
Project/Site
Designer
Project Date 31/07/2023

INPUT DATA												
OS Reference	TM271765						Basic Wind Speed Vb			24.1 m/s		
Site Altitude	52						Pitch			20°		
Sa calculated using	Topography						Obstructions			Included		
MAX DYNAMIC PRESSURE q (kN/m ²)												
Direction (N)	0°	30°	60°	90°	120°	150°	180°	210°	240°	270°	300°	330°
Roof	0.604	0.534	0.551	0.573	0.557	0.664	0.716	0.811	0.938	0.919	0.777	0.631
Sides	0.510	0.451	0.465	0.484	0.470	0.561	0.605	0.685	0.792	0.776	0.656	0.532
Gable	0.604	0.534	0.551	0.573	0.557	0.664	0.716	0.811	0.938	0.919	0.777	0.631





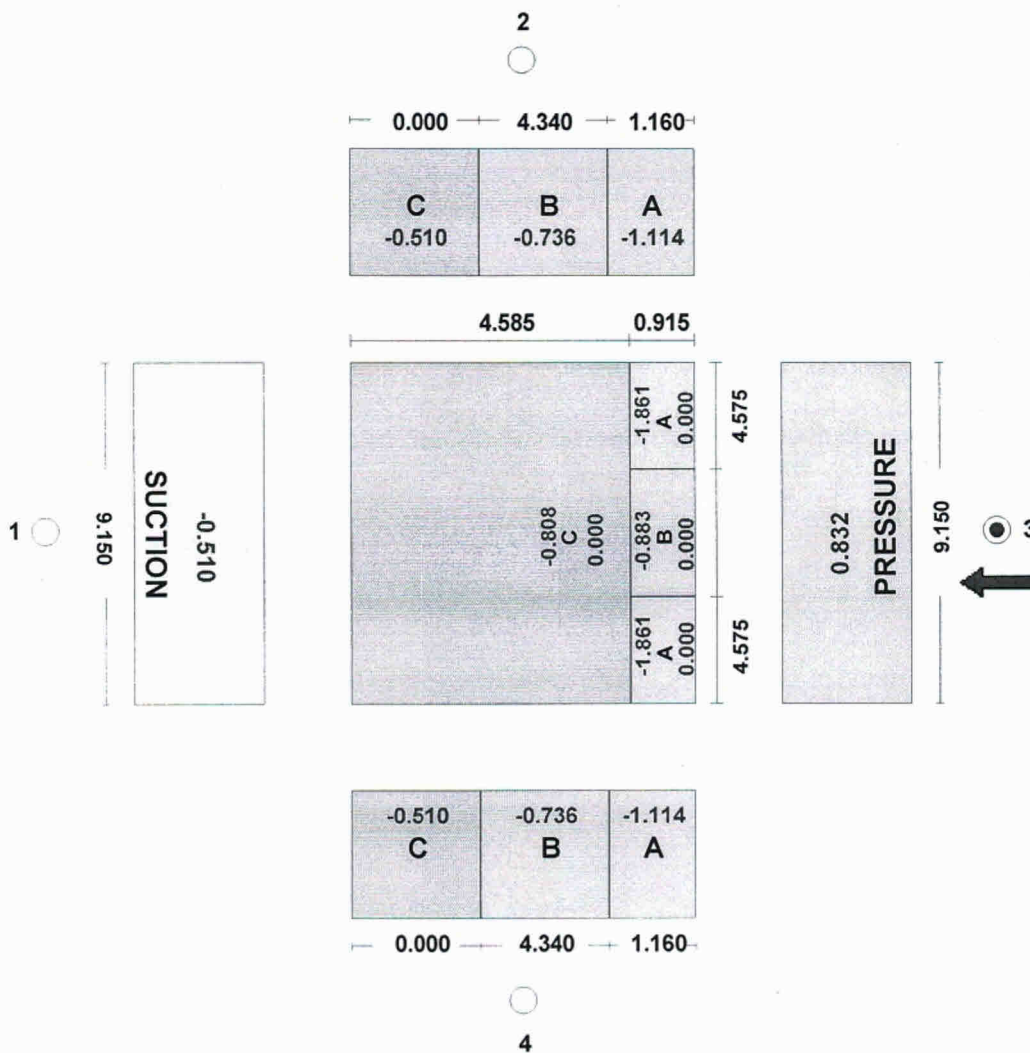
Job No.
 Customer
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Project Date 31/07/2023

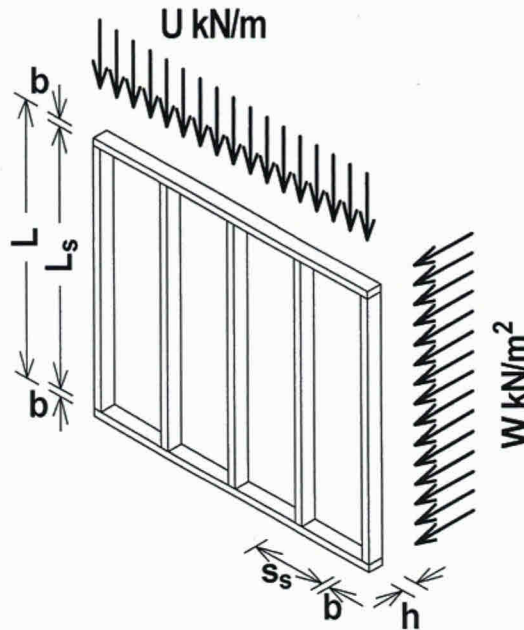
INPUT DATA												
OS Reference	TM271765			Basic Wind Speed Vb				24.1 m/s				
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Gable	0.604	0.534	0.551	0.573	0.557	0.664	0.716	0.811	0.938	0.919	0.777	0.631



Brett Design Partnership 4 Maiden Way Hadleigh, Ipswich Suffolk IP7 5EH	Project Widgeham Barn				Job Ref. 11352	
	Section Studwork				Sheet no./rev. 4	
	Calc. by B. Simmons	Date 31/07/2023	Chk'd by	Date	App'd by	Date

TIMBER STUD DESIGN (BS5268-2:2002)

TEDDS calculation version 1.0.01



Stud details

Stud breadth	$b = 50 \text{ mm}$
Stud depth	$h = 150 \text{ mm}$
Number of studs	$N_s = 1$

Strength class C16 timber (Table 8 BS5268:Pt 2:2002)

Section properties

Cross sectional area	$A = N_s \times b \times h = 7500 \text{ mm}^2$
Section modulus	$Z = N_s \times b \times h^2 / 6 = 187500 \text{ mm}^3$
Moment of inertia in the major axis	$I_x = N_s \times b \times h^3 / 12 = 14062500 \text{ mm}^4$
Moment of inertia in the minor axis	$I_y = N_s \times h \times b^3 / 12 = 1562500 \text{ mm}^4$
Radius of gyration in the major axis	$r_x = \sqrt{I_x / A} = 43.3 \text{ mm}$
Radius of gyration in the minor axis	$r_y = \sqrt{I_y / A} = 14.4 \text{ mm}$

Panel details - Studs restrained by sheathing in the plane of the panel

Panel height	$L = 3800 \text{ mm}$
Stud length	$L_s = L - (2 \times b) = 3700 \text{ mm}$
Standard stud spacing	$s_s = 600 \text{ mm}$
Panel opening	$O = 0 \text{ mm}$
Loaded panel length	$s = \max(s_s, (O + s_s) / 2) = 600 \text{ mm}$
Effective length in the major axis	$L_{ex} = 1.00 \times L_s = 3700 \text{ mm}$
Slenderness ratio	$\lambda = L_{ex} / r_x = 85.45$

Vertical loading details

Wall UDL

Dead loads

$U_{w,d} = 1.90 \text{ kN/m}$

Imposed loads

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Roof UDL	$U_{r,d} = 2.67 \text{ kN/m}$	$U_{r,i} = 1.90 \text{ kN/m}$
Lateral loading details		
Wind loading	$W = 0.92 \text{ kN/m}^2$	
Wind load duration	Short term	
Modification factors		
Section depth factor	$K_7 = (300 \text{ mm} / h)^{0.11} = 1.08$	
Load sharing factor	$K_8 = 1.10$	
Consider combined axial compression and bending under short term loads		
Load duration factor	$K_3 = 1.50$	
Vertical loading	$F = (U_{w,d} + U_{r,d} + U_{r,i}) \times s = 3.88 \text{ kN}$	
Check bending stress		
Bending parallel to grain	$\sigma_m = 5.300 \text{ N/mm}^2$	
Permissible bending stress	$\sigma_{m,adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 9.438 \text{ N/mm}^2$	
Bending moment	$M_{max} = W \times s \times L^2 / 8 = 0.996 \text{ kNm}$	
Applied bending stress	$\sigma_{m,max} = M_{max} / Z = 5.314 \text{ N/mm}^2$	
PASS - Applied bending stress under short term loads is within permissible limits		
Check compressive stress on stud		
Compression member factor	$K_{12} = 0.38$	
Compression parallel to grain	$\sigma_c = 6.800 \text{ N/mm}^2$	
Permissible compressive stress	$\sigma_{c,adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 4.251 \text{ N/mm}^2$	
Applied compressive stress	$\sigma_{c,max} = F / (N_s \times b \times h) = 0.518 \text{ N/mm}^2$	
PASS - Applied compressive stress under short term loads is within permissible limits		
Check compressive stress on rail		
Bearing stress modification factor	$K_4 = 1.20$	
Compression perpendicular to grain (no wane)	$\sigma_{cp1} = 2.200 \text{ N/mm}^2$	
Permissible compressive stress	$\sigma_{cp1,adm} = \sigma_{cp1} \times K_3 \times K_4 = 3.960 \text{ N/mm}^2$	
Applied compressive stress	$\sigma_{cp1,max} = F / (N_s \times b \times h) = 0.518 \text{ N/mm}^2$	
PASS - Applied compressive stress under short term loads is within permissible limits		
Check combined axial compression and bending		
Euler critical stress	$\sigma_e = (\pi^2 \times E_{min}) / \lambda^2 = 7.840 \text{ N/mm}^2$	
Euler coefficient	$K_{eu} = 1 - (1.5 \times \sigma_{c,max} \times K_{12} / \sigma_e) = 0.962$	
Combined axial compression and bending value	$K = \sigma_{m,max} / (\sigma_{m,adm} \times K_{eu}) + \sigma_{c,max} / \sigma_{c,adm} = 0.707 < 1$	
PASS - Combined compressive and bending stresses under short term loads are within permissible limits		
Check stud deflection		
Maximum deflection	$\delta_{adm} = \min(11.1 \text{ mm}, 0.003 \times (L - 2 \times b)) = 11.100 \text{ mm}$	
Bending deflection	$\delta_{max} = 5 \times W \times s \times L^4 / (384 \times E_{mean} \times I_x) = 10.885 \text{ mm}$	
PASS - Deflection due to wind loading is less than permissible limit		
Consider axial compression without bending under medium term loads		
Load duration factor	$K_3 = 1.25$	
Vertical loading	$F = (U_{w,d} + U_{r,d} + U_{r,i}) \times s = 3.88 \text{ kN}$	
Check compressive stress on stud		
Compression member factor	$K_{12} = 0.42$	
Compression parallel to grain	$\sigma_c = 6.800 \text{ N/mm}^2$	
Permissible compressive stress	$\sigma_{c,adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 3.951 \text{ N/mm}^2$	

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Applied compressive stress

$$\sigma_{c_max} = F / (N_s \times b \times h) = 0.518 \text{ N/mm}^2$$

PASS - Applied compressive stress under medium term loads is within permissible limits

Check compressive stress on rail

Bearing stress modification factor

$$K_4 = 1.20$$

Compression perpendicular to grain (no wane)

$$\sigma_{cp1} = 2.200 \text{ N/mm}^2$$

Permissible compressive stress

$$\sigma_{cp1_adm} = \sigma_{cp1} \times K_3 \times K_4 = 3.300 \text{ N/mm}^2$$

Applied compressive stress

$$\sigma_{cp1_max} = F / (N_s \times b \times h) = 0.518 \text{ N/mm}^2$$

PASS - Applied compressive stress under medium term loads is within permissible limits

Consider axial compression without bending under long term loads

Load duration factor

$$K_3 = 1.00$$

Vertical loading

$$F = (U_{w_d} + U_{r_d}) \times s = 2.74 \text{ kN}$$

Check compressive stress on stud

Compression member factor

$$K_{12} = 0.47$$

Compression parallel to grain

$$\sigma_c = 6.800 \text{ N/mm}^2$$

Permissible compressive stress

$$\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 3.541 \text{ N/mm}^2$$

Applied compressive stress

$$\sigma_{c_max} = F / (N_s \times b \times h) = 0.366 \text{ N/mm}^2$$

PASS - Applied compressive stress under long term loads is within permissible limits

Check compressive stress on rail

Bearing stress modification factor

$$K_4 = 1.20$$

Compression perpendicular to grain (no wane)

$$\sigma_{cp1} = 2.200 \text{ N/mm}^2$$

Permissible compressive stress

$$\sigma_{cp1_adm} = \sigma_{cp1} \times K_3 \times K_4 = 2.640 \text{ N/mm}^2$$

Applied compressive stress

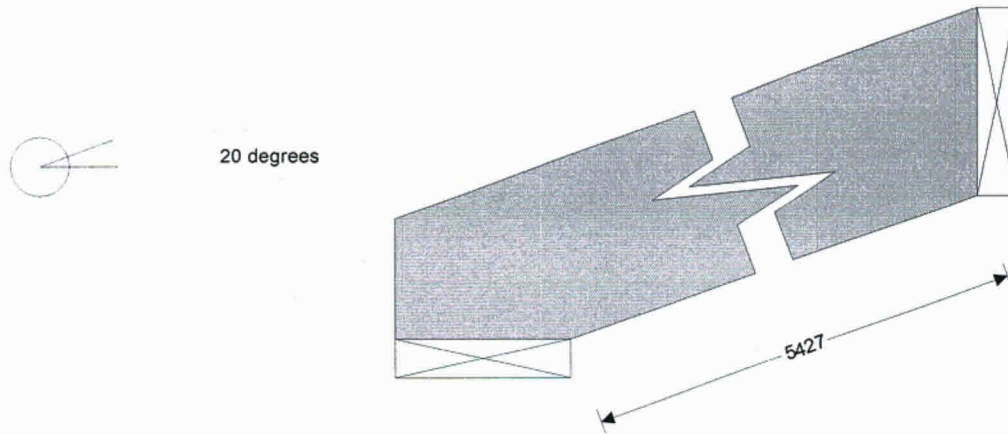
$$\sigma_{cp1_max} = F / (N_s \times b \times h) = 0.366 \text{ N/mm}^2$$

PASS - Applied compressive stress under long term loads is within permissible limits

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	Section Rafters				Sheet no./rev. 7	
	Calc. by B. Simmons	Date 31/07/2023	Chk'd by	Date	App'd by	Date

TIMBER RAFTER DESIGN (BS5268-2:2002)

TEDDS calculation version 1.0.03



Rafter details

Breadth of timber sections	b = 50 mm
Depth of timber sections	h = 225 mm
Rafter spacing	s = 450 mm
Rafter slope	$\alpha = 20.0$ deg
Clear span of rafter on horizontal	L_{clh} = 5100 mm
Clear span of rafter on slope	L_{cl} = L_{clh} / cos(α) = 5427 mm
Rafter span	Single span
Timber strength class	C16

Section properties

Cross sectional area of rafter	A = b × h = 11250 mm²
Section modulus	Z = b × h² / 6 = 421875 mm³
Second moment of area	I = b × h³ / 12 = 47460937 mm⁴
Radius of gyration	r = $\sqrt{I / A}$ = 65.0 mm

Loading details

Rafter self weight	F_j = b × h × ρ_{char} × g_{acc} = 0.03 kN/m
Dead load on slope	F_d = 0.70 kN/m²
Imposed load on plan	F_u = 0.75 kN/m²
Imposed point load	F_p = 0.90 kN

Modification factors

Section depth factor	K₇ = (300 mm / h)^{0.11} = 1.03
Load sharing factor	K₈ = 1.10

Consider long term load condition

Load duration factor	K₃ = 1.00
Total UDL perpendicular to rafter	F = F_d × cos(α) × s + F_j × cos(α) = 0.328 kN/m
Notional bearing length	L_b = F × L_{cl} / [2 × (b × σ_{op1} × K₈ - F)] = 7 mm
Effective span	L_{eff} = L_{cl} + L_b = 5435 mm

Check bending stress

Bending stress parallel to grain	$\sigma_m = 5.300$ N/mm²
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Permissible bending stress

$$\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 6.017 \text{ N/mm}^2$$

Applied bending stress

$$\sigma_{m_max} = F \times L_{eff}^2 / (8 \times Z) = 2.872 \text{ N/mm}^2$$

PASS - Applied bending stress within permissible limits

Check compressive stress parallel to grain

Compression stress parallel to grain

$$\sigma_c = 6.800 \text{ N/mm}^2$$

Minimum modulus of elasticity

$$E_{min} = 5800 \text{ N/mm}^2$$

Compression member factor

$$K_{12} = 0.49$$

Permissible compressive stress

$$\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 3.630 \text{ N/mm}^2$$

Applied compressive stress

$$\sigma_{c_max} = F \times L_{eff} \times (\cot(\alpha) + 3 \times \tan(\alpha)) / (2 \times A) = 0.304 \text{ N/mm}^2$$

PASS - Applied compressive stress within permissible limits

Check combined bending and compressive stress parallel to grain

Euler stress

$$\sigma_e = \pi^2 \times E_{min} / \lambda^2 = 8.176 \text{ N/mm}^2$$

Euler coefficient

$$K_{eu} = 1 - (1.5 \times \sigma_{c_max} \times K_{12} / \sigma_e) = 0.973$$

Combined axial compression and bending check

$$\sigma_{m_max} / (\sigma_{m_adm} \times K_{eu}) + \sigma_{c_max} / \sigma_{c_adm} = 0.574 < 1$$

PASS - Combined compressive and bending stresses are within permissible limits

Check shear stress

Shear stress parallel to grain

$$\tau = 0.670 \text{ N/mm}^2$$

Permissible shear stress

$$\tau_{adm} = \tau \times K_3 \times K_8 = 0.737 \text{ N/mm}^2$$

Applied shear stress

$$\tau_{max} = 3 \times F \times L_{eff} / (4 \times A) = 0.119 \text{ N/mm}^2$$

PASS - Applied shear stress within permissible limits

Check deflection

Permissible deflection

$$\delta_{adm} = 0.003 \times L_{eff} = 16.304 \text{ mm}$$

Bending deflection

$$\delta_b = 5 \times F \times L_{eff}^4 / (384 \times E_{mean} \times I) = 8.924 \text{ mm}$$

Shear deflection

$$\delta_s = 12 \times F \times L_{eff}^2 / (5 \times E_{mean} \times A) = 0.235 \text{ mm}$$

Total deflection

$$\delta_{max} = \delta_b + \delta_s = 9.159 \text{ mm}$$

PASS - Total deflection within permissible limits

Consider medium term load condition

Load duration factor

$$K_3 = 1.25$$

Total UDL perpendicular to rafter

$$F = [F_u \times \cos(\alpha)^2 + F_d \times \cos(\alpha)] \times s + F_j \times \cos(\alpha) = 0.626 \text{ kN/m}$$

Notional bearing length

$$L_b = F \times L_{cl} / [2 \times (b \times \sigma_{cp1} \times K_8 - F)] = 14 \text{ mm}$$

Effective span

$$L_{eff} = L_{cl} + L_b = 5441 \text{ mm}$$

Check bending stress

Bending stress parallel to grain

$$\sigma_m = 5.300 \text{ N/mm}^2$$

Permissible bending stress

$$\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 7.522 \text{ N/mm}^2$$

Applied bending stress

$$\sigma_{m_max} = F \times L_{eff}^2 / (8 \times Z) = 5.493 \text{ N/mm}^2$$

PASS - Applied bending stress within permissible limits

Check compressive stress parallel to grain

Compression stress parallel to grain

$$\sigma_c = 6.800 \text{ N/mm}^2$$

Minimum modulus of elasticity

$$E_{min} = 5800 \text{ N/mm}^2$$

Compression member factor

$$K_{12} = 0.43$$

Permissible compressive stress

$$\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 4.059 \text{ N/mm}^2$$

Applied compressive stress

$$\sigma_{c_max} = F \times L_{eff} \times (\cot(\alpha) + 3 \times \tan(\alpha)) / (2 \times A) = 0.581 \text{ N/mm}^2$$

PASS - Applied compressive stress within permissible limits

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Check combined bending and compressive stress parallel to grain

Euler stress $\sigma_e = \pi^2 \times E_{min} / \lambda^2 = 8.156 \text{ N/mm}^2$
 Euler coefficient $K_{eu} = 1 - (1.5 \times \sigma_{c_max} \times K_{12} / \sigma_e) = 0.954$
 Combined axial compression and bending check $\sigma_{m_max} / (\sigma_{m_adm} \times K_{eu}) + \sigma_{c_max} / \sigma_{c_adm} = 0.909 < 1$

PASS - Combined compressive and bending stresses are within permissible limits

Check shear stress

Shear stress parallel to grain $\tau = 0.670 \text{ N/mm}^2$
 Permissible shear stress $\tau_{adm} = \tau \times K_3 \times K_8 = 0.921 \text{ N/mm}^2$
 Applied shear stress $\tau_{max} = 3 \times F \times L_{eff} / (4 \times A) = 0.227 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

Check deflection

Permissible deflection $\delta_{adm} = 0.003 \times L_{eff} = 16.324 \text{ mm}$
 Bending deflection $\delta_b = 5 \times F \times L_{eff}^4 / (384 \times E_{mean} \times I) = 17.114 \text{ mm}$
 Shear deflection $\delta_s = 12 \times F \times L_{eff}^2 / (5 \times E_{mean} \times A) = 0.449 \text{ mm}$
 Total deflection $\delta_{max} = \delta_b + \delta_s = 17.564 \text{ mm}$

FAIL - Total deflection exceeds permissible limits

Consider short term load condition

Load duration factor $K_3 = 1.50$
 Total UDL perpendicular to rafter $F = F_d \times \cos(\alpha) \times s + F_j \times \cos(\alpha) = 0.328 \text{ kN/m}$
 Notional bearing length $L_b = [F \times L_{cl} + F_p \times \cos(\alpha)] / [2 \times (b \times \sigma_{cp1} \times K_8 - F)] = 11 \text{ mm}$
 Effective span $L_{eff} = L_{cl} + L_b = 5438 \text{ mm}$

Check bending stress

Bending stress parallel to grain $\sigma_m = 5.300 \text{ N/mm}^2$
 Permissible bending stress $\sigma_{m_adm} = \sigma_m \times K_3 \times K_7 \times K_8 = 9.026 \text{ N/mm}^2$
 Applied bending stress $\sigma_{m_max} = F \times L_{eff}^2 / (8 \times Z) + F_p \times \cos(\alpha) \times L_{eff} / (4 \times Z) = 5.601 \text{ N/mm}^2$

PASS - Applied bending stress within permissible limits

Check compressive stress parallel to grain

Compression stress parallel to grain $\sigma_c = 6.800 \text{ N/mm}^2$
 Minimum modulus of elasticity $E_{min} = 5800 \text{ N/mm}^2$
 Compression member factor $K_{12} = 0.39$
 Permissible compressive stress $\sigma_{c_adm} = \sigma_c \times K_3 \times K_8 \times K_{12} = 4.382 \text{ N/mm}^2$
 Applied compressive stress $\sigma_{c_max} = F \times L_{eff} \times (\cot(\alpha) + 3 \times \tan(\alpha)) / (2 \times A) + F_p \times \sin(\alpha) / A = 0.332 \text{ N/mm}^2$

PASS - Applied compressive stress within permissible limits

Check combined bending and compressive stress parallel to grain

Euler stress $\sigma_e = \pi^2 \times E_{min} / \lambda^2 = 8.166 \text{ N/mm}^2$
 Euler coefficient $K_{eu} = 1 - (1.5 \times \sigma_{c_max} \times K_{12} / \sigma_e) = 0.976$
 Combined axial compression and bending check $\sigma_{m_max} / (\sigma_{m_adm} \times K_{eu}) + \sigma_{c_max} / \sigma_{c_adm} = 0.711 < 1$

PASS - Combined compressive and bending stresses are within permissible limits

Check shear stress

Shear stress parallel to grain $\tau = 0.670 \text{ N/mm}^2$
 Permissible shear stress $\tau_{adm} = \tau \times K_3 \times K_8 = 1.106 \text{ N/mm}^2$
 Applied shear stress $\tau_{max} = 3 \times F \times L_{eff} / (4 \times A) + 3 \times F_p \times \cos(\alpha) / (2 \times A) = 0.232 \text{ N/mm}^2$

PASS - Applied shear stress within permissible limits

Brett Design Partnership 4 Maiden Way Hadleigh, Ipswich Suffolk IP7 5EH	Project				Job Ref.	
	Widgeham Barn				11352	
	Section				Sheet no./rev.	
Rafters				10		
Calc. by	Date	Chk'd by	Date	App'd by	Date	
B. Simmons	31/07/2023					

Check deflection

Permissible deflection

$$\delta_{adm} = 0.003 \times L_{eff} = \mathbf{16.315 \text{ mm}}$$

Bending deflection

$$\delta_b = L_{eff}^3 \times (5 \times F \times L_{eff} / 384 + F_p \times \cos(\alpha) / 48) / (E_{mean} \times I) = \mathbf{15.732 \text{ mm}}$$

Shear deflection

$$\delta_s = 12 \times L_{eff} \times (F \times L_{eff} + 2 \times F_p \times \cos(\alpha)) / (5 \times E_{mean} \times A) = \mathbf{0.458 \text{ mm}}$$

Total deflection

$$\delta_{max} = \delta_b + \delta_s = \mathbf{16.190 \text{ mm}}$$

PASS - Total deflection within permissible limits